

Computational Mechanics: What Do We Do?

An Introduction of Division of Mechanics at CSRC

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Universidade Federal do ABC

October 16, 2017

1 Vision, Objectives, and Means

2 Personnel

- Prof. Xiaolong Deng: DNS of Interfacial Dynamics
- Prof. Yang Ding: Bio-Mechanics and Complex Fluids
- Prof. Shujie Li: High-Order Methods, HPC
- Prof. Weidong Li: Kinetic Methods
- Prof. Li-Shi Luo: Droplet and Film

3 Some Ongoing Research

- DNS of Turbulence
- Modeling/Simulation of Molecular Flows

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In **classical continuum mechanics** of fluids and solids, no need to consider both quantum and relativistic effects, *i.e.*, in the limits of $\hbar = 0$ and $c = \infty$. Quantum ($\hbar = 1$), relativistic ($c = 1$), and other effects may have to be considered in some non-equilibrium systems.

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It is imperative for us to break the barriers between the “mechanics” and other realms of modern physics so the “*mechanics*” would no longer be just “*continuum*” or “*classical*”. This requires multi-disciplinary knowledge.

$\hbar = 1$ $c = \infty$	$\hbar = 1$ $c = 1$
$\hbar = 0$ $c = \infty$	$\hbar = 0$ $c = 1$

Mission

DoM has written a **5-year** research plan based on its vision and resources, including the following specific objectives:

- **Mission**: to conduct basic research in the frontiers of modern **computational** mechanics in its broadest sense — **the 3rd Pillar**;
- **Character**: interdisciplinary research involving physics, applied mathematics, and computing;
- **Focuses**: modeling and simulation of **multi-scale, multi-physics** phenomena observed in **fluid, soft matter, granular material**, and **solid**, which may or may not be adequately described by macroscopic theories;
- **Education and Training**: our research strength and excellence will drive our educational program to train **indigenous** students and junior researchers;
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Modeling and simulation of the following systems:

- thermochemically nonequilibrium flows
- molecular micro flows
- multi-phase and multi-component flows
- interfacial dynamics
- Stokes, incompressible and compressible flows
- multi-scale and multi-physics and complex fluids
- granular flows, bio-mechanics, bio-robotics

Specific Methodologies and Means

General areas:

- PDE's (modeling) and its numerical solutions by means of HPC;
- Large-scale scientific computing, high-performance and parallel computing, emerging computing technology (MIC, GPUs);
- Algorithms and numerical analysis.

Specific methods and techniques:

- Numerical methods for PDEs: finite-volume, finite-difference, spectral and spectral element, discontinuous Galerkin, Stokelets, kinetic methods, high-order/high-resolution methods, ...
- Diffuse-interface and interface tracking methods
- Mesh/grid generation and adaptive mesh refinement
- Discrete element method, Molecular dynamics
- FMM for solving integral equations

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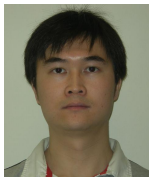
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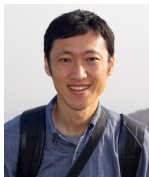
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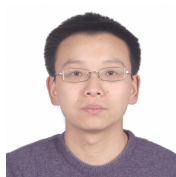
Prof. Xiaolong Deng



Prof. Yang Ding



Dr. Shujie Li



Dr. Weidong Li

Chair Professor:	1
Tenure-track faculty:	2
Research faculty:	2
Associated members:	4
Post-doctoral research associates:	3
Graduate students:	6
Long-term collaborators/visitors:	...

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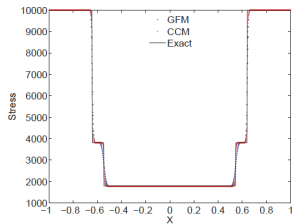
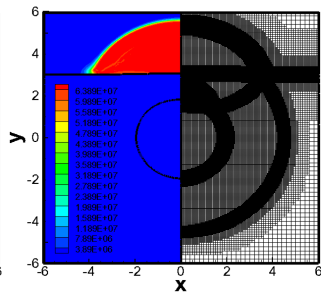
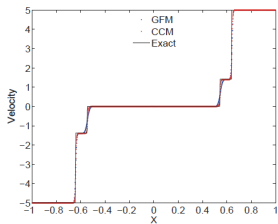
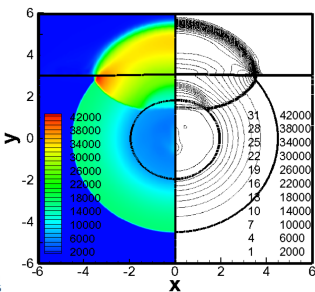
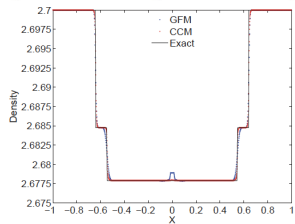
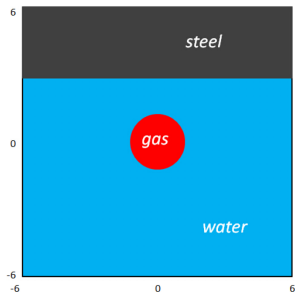
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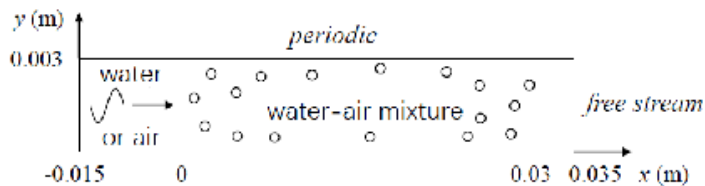
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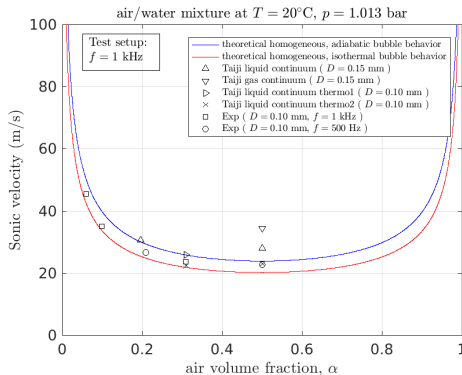
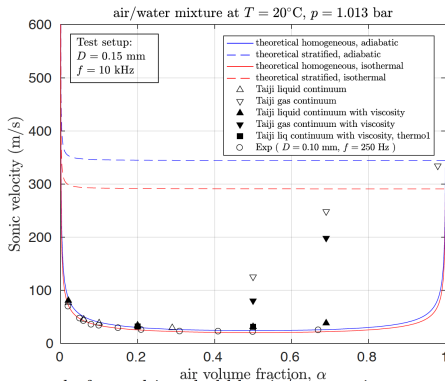
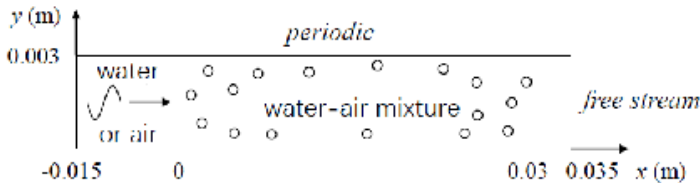
Deng XL: Fluid-Elastic-Perfectly Plastic Interfaces



Deng XL: Sound Speed in Gas-Water Two-Phase Flows



Deng XL: Sound Speed in Gas-Water Two-Phase Flows



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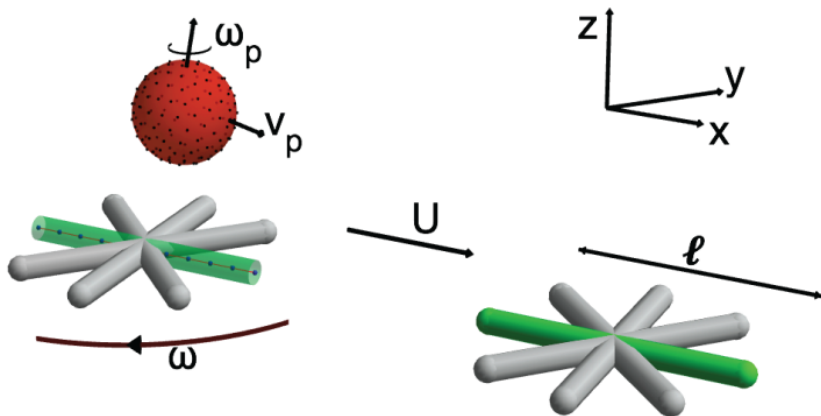
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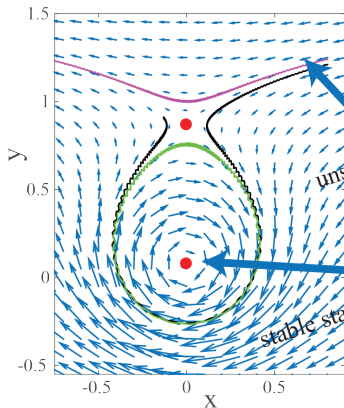
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Numerical study of particle-trapping and transport by a nano-wire:¹

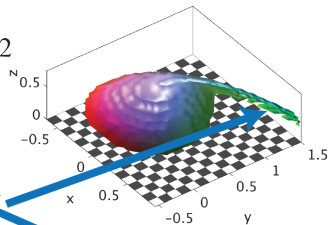


¹In collaboration with L. Zhao (CWRU) and L. Zhang (CHKU).

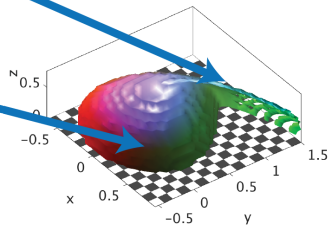
Displacement Field



$R=0.2$

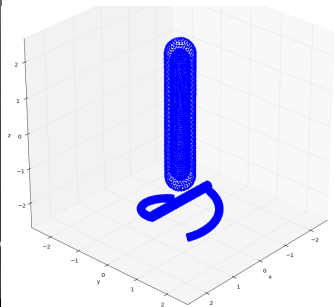
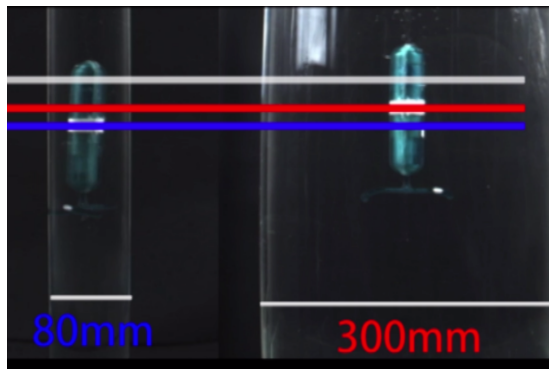


$R=0$

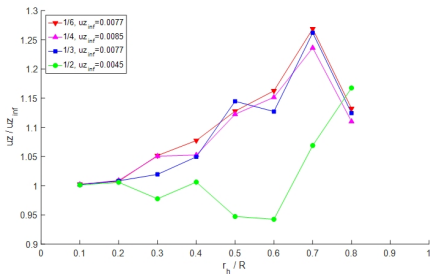
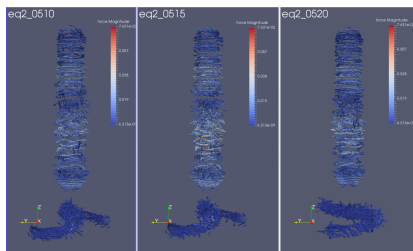


Capturing Region

Experimental and numerical study of helix swimmers inside a tube



Experimental and numerical study of helix swimmers inside a tube



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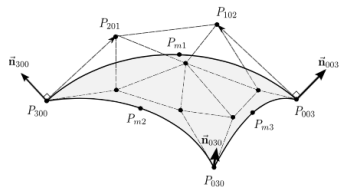
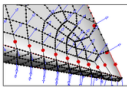
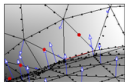
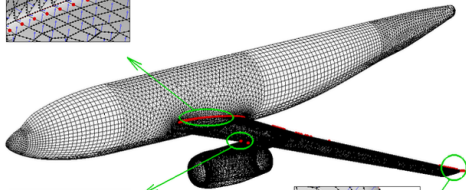
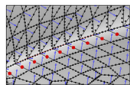
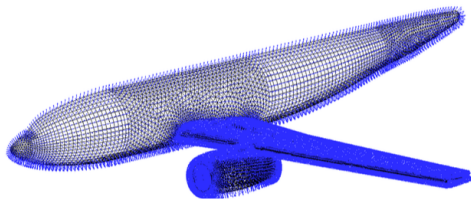
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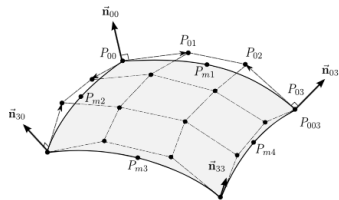
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Li Shujie: High-Order Methods on HPC



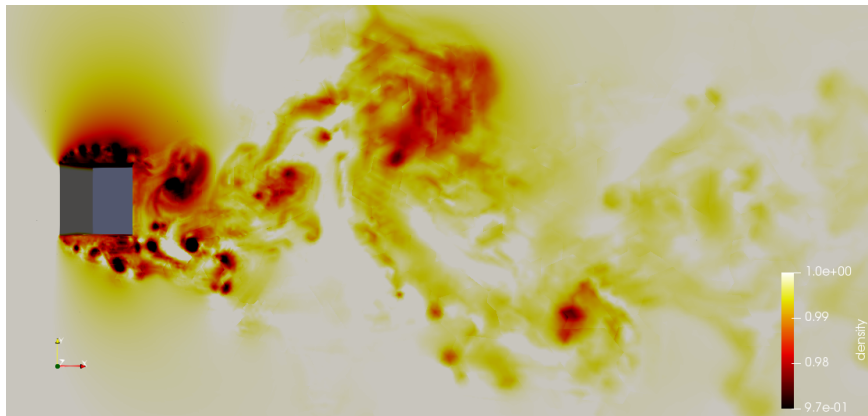
(a) Bézier triangle



(b) Bézier quadrilateral

Li Shujie: High-Order Methods on HPC

- Predictor-Corrector Exponential time integrator scheme (PCEXP) extended to simulate 3D NS equations with variable accuracy
- Implicit LES of turbulence flow past a square cylinder at $Re = 2,200$



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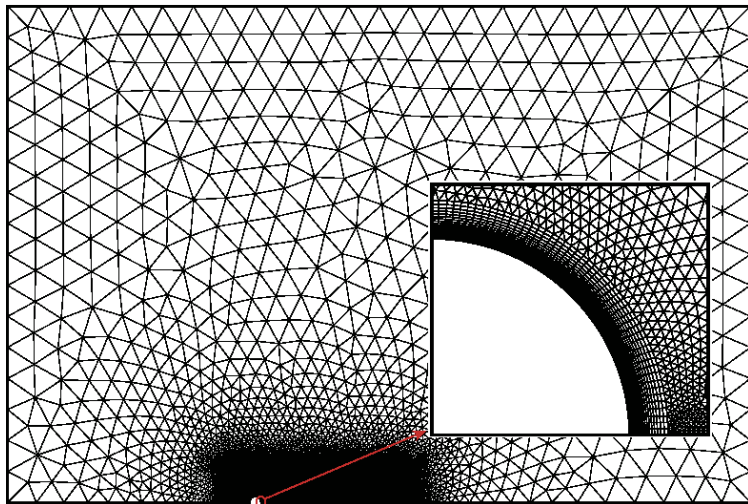
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Li WD (李维东): FV-LBE on Unstructured Mesh

Explicit and implicit LBE-FV method on unstructured meshes:²



²W.D. Li & L.-S. Luo. *Comm. Comput. Phys.* **20**(2):301–324 (2016);
J. Comput. Phys. **327**:503–518 (2016).

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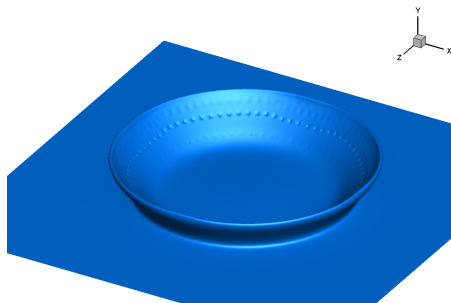
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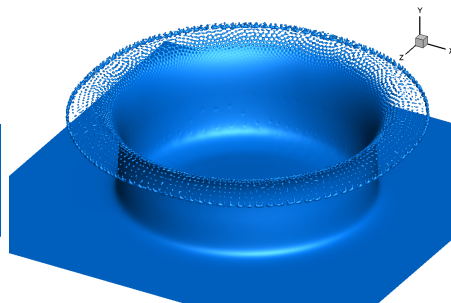
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Luo LS: Drop Splashing on a Wet Surface



(a)



(b)

Drop impact on a wet surface at $t^* = 2.0$, $R_\rho = 500$, $We = 8000$, $Re = 1000$. (a) $R_\mu = 400$; (b) $R_\mu = 40$.

Droplet Coalescence: Simulation *vs.* Experiment

LB numerical *vs.* experimental results

$$R_\rho = 1.316$$

$$R_\mu = 0.5$$

$$\text{Bo} = 9.59 \times 10^{-2}$$

$$\text{Oh} = 5.53 \times 10^{-3}$$

The evolution in

$$0 \leq t^* \leq 0.890$$

with time increment

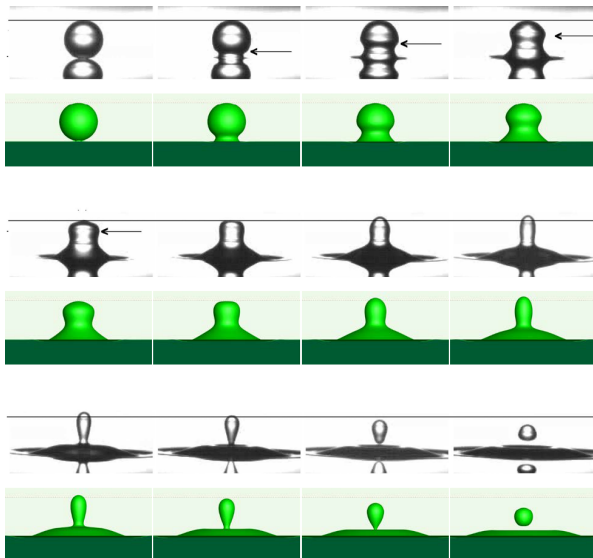
$$\Delta t^* = 0.081, \text{ which}$$

corresponds to 542

microseconds in exper-

iments [Chen, Mandre, Feng,

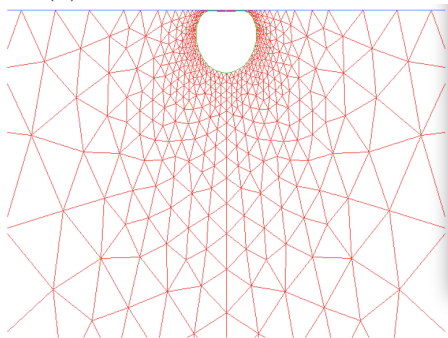
Phys. Fluids 18:051705 (2006)].



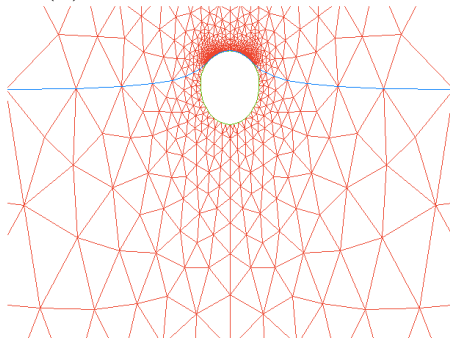
Simulation: Bubble Interact with Interfaces

Objective: To study thin films between interfaces ...

(a) bubble interact with wall



(b) interact with an interface



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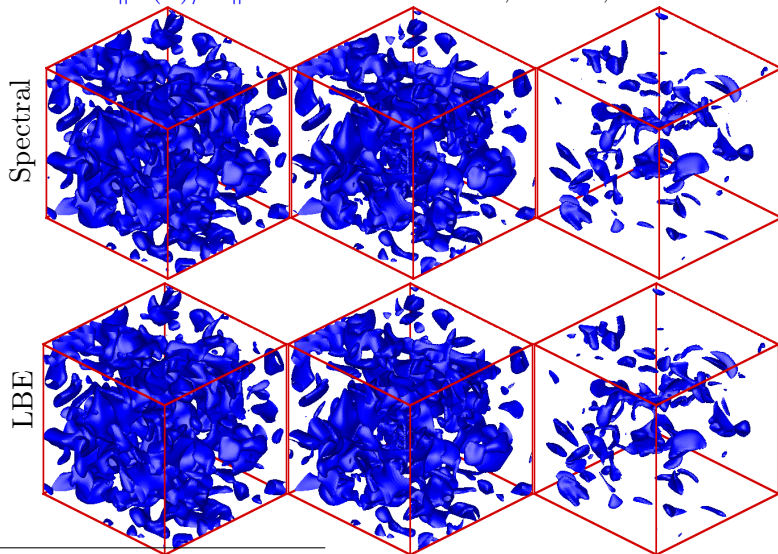
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Decaying Homogenous Isotropic Turbulence $Re_\lambda = 24.37$

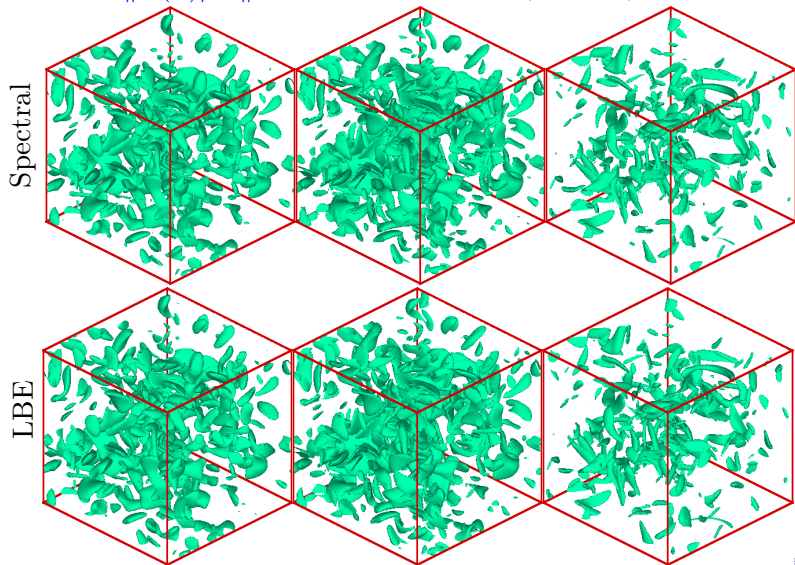
iso-surface of $\|\mathbf{u}(t')/u'\| = 2.0$ at $t' = 0.1348, 0.2359, 0.573$.³



³Y. Peng, W. Liao, L.-S. Luo, L.-P. Wang. *Comput. Fluids* **39**(4):568–591 (2010).

Decaying Homogenous Isotropic Turbulence $Re_\lambda = 24.37$

iso-surface of $\|\omega(t')/u'\| = 13.0$ at $t' = 0.1348, 0.2359, 0.573$:



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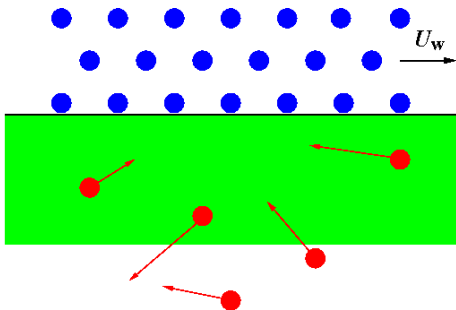
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Isothermal Rarefied Couette Flows

Two parallel plate of separation H moving in opposite directions with speed U_w , gas and wall molecules are Argon ones with 12-6 Lennard-Jones potential:

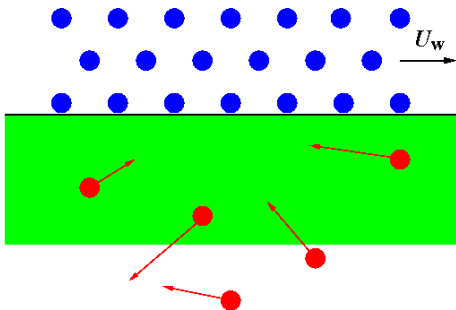
$$V(r^*) = 4\epsilon \left(\frac{1}{r^{*12}} - \frac{1}{r^{*6}} \right), \quad r^* := \frac{r_{ij}}{\sigma} = \frac{\|\mathbf{r}_i - \mathbf{r}_j\|}{\sigma} \quad (1)$$



Isothermal Rarefied Couette Flows

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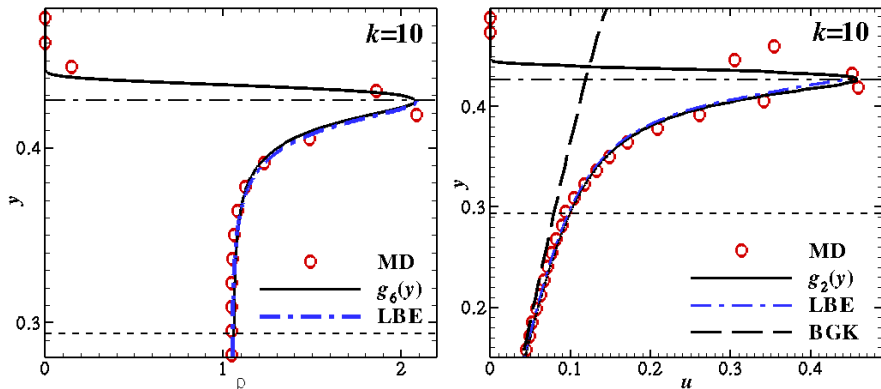


Multi-scale Features:

- Near the walls (greed region) $(\frac{1}{2} \geq y \geq \frac{1}{2} - \frac{3\sigma}{2H})$:
van der Waals forces dominant
molecular flow (σ , ϵ)
- Away from the walls $(\frac{H-3\sigma}{2H} \geq y \geq \frac{3\sigma-H}{2H})$:
a kinetic problem (ℓ , Kn)

Results: $k = 10.0$

The results of MD, LBE, and the linearized Boltzmann equation:⁴



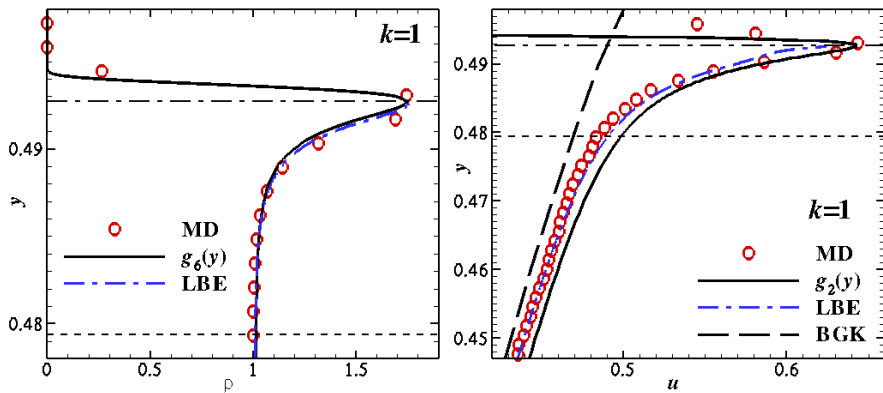
CPU times:

MD $\sim O(\text{day}) \gg$ Linearized BE $\approx O(\text{hour}) \gg$ LBE $\lesssim O(\text{minute})$

⁴W. Li, L.-S. Luo, J. Shen. *Comput. Fluids* 111:18–32 (2015).

Results: $k = 1.0$

The results of MD, LBE, and the linearized Boltzmann equation:



CPU times:

MD $> O(\text{day}) \gg$ Linearized BE $\approx O(\text{hour}) \gg$ LBE $\lesssim O(\text{minute})$

Thanks! Questions?

"YOU WANT PROOF?
I'LL GIVE YOU PROOF!"

